

8.3

Define and Use Zero and Negative Exponents

Goal • Use zero and negative exponents.

Your Notes

| DEFINITION OF ZERO AND NEGATIVE EXPONENTS | | |
|---|---|-------------------------------------|
| Words | Algebra | Example |
| a to the zero power is 1. | $a^0 = \underline{\hspace{1cm}}, a \neq 0$ | $5^0 = \underline{\hspace{1cm}}$ |
| a^{-n} is the reciprocal of a^n . | $a^{-n} = \underline{\hspace{1cm}}, a \neq 0$ | $2^{-1} = \underline{\hspace{1cm}}$ |
| a^n is the reciprocal of a^{-n} . | $a^n = \underline{\hspace{1cm}}, a \neq 0$ | $2 = \underline{\hspace{1cm}}$ |

Example 1 Use definition of zero and negative exponents

Evaluate the expression.

- a. $2^{-3} = \underline{\hspace{1cm}}$ Definition of $\underline{\hspace{1cm}}$
 $\underline{\hspace{1cm}}$ $\underline{\hspace{1cm}}$
 $= \underline{\hspace{1cm}}$ Evaluate exponent.
- b. $(-10)^0 = \underline{\hspace{1cm}}$ Definition of $\underline{\hspace{1cm}}$
- c. $\left(\frac{1}{4}\right)^{-3} = \underline{\hspace{1cm}}$ Definition of $\underline{\hspace{1cm}}$
 $\underline{\hspace{1cm}}$ $\underline{\hspace{1cm}}$
 $= \underline{\hspace{1cm}}$ Evaluate exponent.
 $= \underline{\hspace{1cm}}$ Simplify.
- d. $0^{-7} = \underline{\hspace{1cm}}$ a^{-n} is defined only for
a $\underline{\hspace{1cm}}$ number a .

Your Notes

PROPERTIES OF EXPONENTS

Let a and b be real numbers, and let m and n be integers.

$a^m \cdot a^n = a$ _____ **property**

$(a^m)^n = a$ _____ **property**

$(ab)^m =$ _____ **property**

$\frac{a^m}{a^n} = a$ _____, $a \neq 0$ _____ **property**

$\left(\frac{a}{b}\right)^m =$ _____, $b \neq 0$ _____ **property**

Example 2 Evaluate exponential expressions

Evaluate the expression.

a. $(-5)^4 \cdot (-5)^{-4} =$ _____ **Product of powers property**
 = _____ **exponents.**
 = _____ **Definition of**

b. $(5^{-2})^{-2} =$ _____ **property**
 = _____ **exponents.**
 = _____ **Evaluate power.**

c. $\frac{1}{4^{-2}} =$ _____ **Definition of**
 = _____ **Evaluate power.**

d. $\frac{3^2}{3^{-1}} =$ _____ **property**
 = _____ **exponents.**
 = _____ **Evaluate power.**

Your Notes

✔ **Checkpoint** Evaluate the expression.

| | |
|------------------------------------|-----------------------|
| 1. $\left(\frac{1}{8}\right)^{-1}$ | 2. $\frac{1}{3^{-2}}$ |
| 3. $\frac{6^{-1}}{6}$ | 4. $(5^{-1})^2$ |

Example 3 Use properties of exponents

Simplify the expression $\frac{2w^{-3}x}{(2wx)^2}$. Write your answer using only positive exponents.

Solution

$$\begin{aligned} \frac{2w^{-3}x}{(2wx)^2} &= \text{_____} && \text{Definition of negative exponents} \\ &= \text{_____} && \text{_____ property} \\ &= \text{_____} && \text{_____ property} \\ &= \text{_____} && \text{_____ property} \end{aligned}$$

✔ **Checkpoint** Simplify the expression.

| | |
|-----------------------------|-------------------|
| 5. $\frac{6fg^{-4}}{2f^2g}$ | 6. $(3yz^2)^{-2}$ |
|-----------------------------|-------------------|

Homework