3.6 Solving Multi-Step Inequalities

Goal: Solve multi-step inequalities.

Example 1 *Writing and Solving a Multi-Step Inequality*

Charity Walk You are participating in a charity walk. You want to raise at least $500 for the charity. You already have $175 by asking people to pledge $25 each. How many more $25 pledges do you need?

Solution

Let p represent the number of additional pledges. Write a verbal model.

$$\boxed{} + \boxed{} \cdot \boxed{} \geq \boxed{}$$

$\boxed{} + \boxed{} \geq \boxed{}$ Substitute.

$\boxed{} + \boxed{} - \boxed{} \geq \boxed{} - \boxed{}$ Subtract $\boxed{}$ from each side.

$\boxed{} \geq \boxed{}$ Simplify.

$\dfrac{\boxed{}}{\boxed{}} \geq \dfrac{\boxed{}}{\boxed{}}$ Divide each side by $\boxed{}$.

$p \geq \boxed{}$ Simplify.

Answer: You need at least $\boxed{}$ more $25 pledges.

✔ *Checkpoint*

1. Look back at Example 1. Suppose you wanted to raise at least $620 and you already have raised $380 by asking people to pledge $20 each. How many more $20 pledges do you need?

Example 2   *Solving a Multi-Step Inequality*

$$\frac{x}{-3} - 9 < -7$$ Original inequality

$$\frac{x}{-3} - 9 + \boxed{} < -7 + \boxed{}$$ Add $\boxed{}$ to each side.

$$\frac{x}{-3} < \boxed{}$$ Simplify.

$$\boxed{}\left(\frac{x}{-3}\right)\boxed{}\boxed{} \cdot \boxed{}$$ Multiply each side by $\boxed{}$.
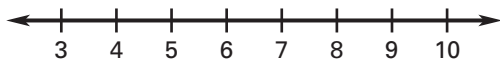Reverse inequality symbol.

$$x \boxed{} \boxed{}$$ Simplify.

✔ *Checkpoint*   **Solve the inequality. Then graph the solution.**
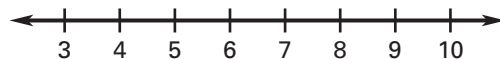
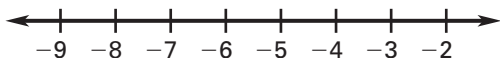**2.** $2x + 9 < 25$

3. $-3 \geq \frac{x}{-4} - 2$

4. $2 > -4 - x$

5. $\frac{x}{2} + 4 \leq 9$